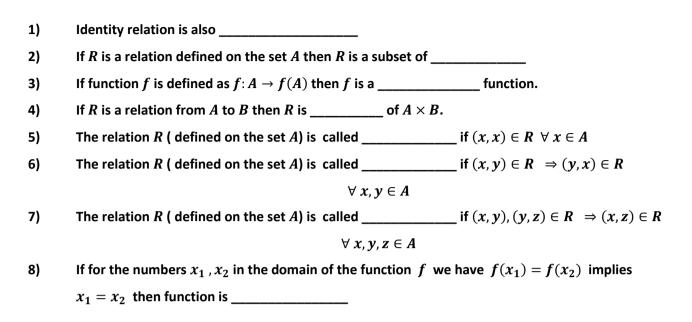


# <u>UNIT –</u> I <u>RELATIONS & FUNCTIONS</u> <u>Multiple Choice Questions(1 Mark)</u>



1	Relation $R = \{(x, y) : x \le y, x, y \in \mathbb{Z}\}$ is
	(a)Reflexive and symmetric relation (bSymmetric and transitive relation
	(c)Equivalence relation(d)Reflexive and transitiverelation
2	Which of the following relations defined on set $A = \{1, 2, 3\}$ is reflexive but neither symmetric nor
	transitive :
	$(a)R = \{(1, 1), (2, 2), (3, 3)\} $ $(b)R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3)\}$
	(c) $R = \{(1,2), (1,3), (2,3), (3,1), (2,1)\}$ (d) $R = \{(1,2), (2,3), (1,3), (2,1)\}$
3	Function defined by $f: R  o R$ , $f(x) = x^3$ is :
	(a)only one-one (b)only onto
	(c)one-one and onto (d)neither one-one nor onto
4	Function defined by $f:\mathbb{R} o\mathbb{R}$ , $f(x)=x^2$ is :
	(a)only one-one (b)only onto
	(c)one-one and onto (d)neither one-one nor onto
5	Relation $R = \{(x, x), (y, y), (x, y), (y, x)\}$ defined on the set $A = \{x, y\}$ is :
	(a)Only Reflexive relation (b)Only Symmetric relation
	(c)Only Transitive relation (d)Equivalence relation
~	
6	Relation $R = \{(x, y) : x < y, x, y \in \mathbb{Z}\}$ is
	(a)Only Reflexive relation (b)Only Symmetric relation
_	(c)Only Transitive relation (d)Equivalence relation
7	Relation $R = \{(x, y) : x < y^2 \text{ where } x, y \in \mathbb{R} \}$ is
	(a)Reflexive but not symmetric (b)Symmetric and transitive but not Reflexive
	(c)Reflexive and Symmetric (d)Neither reflexive nor symmetric nor transitive
8	If $A = \{1, 4, 9, 16, 25, \dots \}$ then function defined by $f : \mathbb{Z} \rightarrow A$ , $f(x) = x^2$ is
	(a)only one-one (b)only onto
	(c)function is not defined(d)neither one-one nor onto
9	If $A = \{0, 1, 4, 9, 16, 25,, \}$ then function defined by $f : \mathbb{N} \to A$ , $f(x) = x^2$ is
	(a)one-one but not onto(b)onto but not one-one
	(c)one-one and onto (d)neither one-one nor onto
10	Function $f: \mathbb{R} \to \mathbb{R}$ , $f(x) = \frac{3-7x}{2}$ is:
	(a)one-one but not onto (b)onto but not one-one
	(c)one-one and onto (d)neither one-one nor onto
11	If $A = \{0, 1, 4, 9, 16, 25,, \}$ then function defined by $f : \mathbb{Z} \to A$ , $f(x) = x^2$ is
	(a)one-one but not onto (b)onto but not one-one
	(c)one-one and onto (d)neither one-one nor onto
12	If $A = \{1, 4, 9, 16, 25, \dots, \}$ then function defined by $f : \mathbb{N} \to A$ , $f(x) = x^2$ is
	(a)only one-one (b)only onto
	(c)one-one and onto (d)neither one-one nor onto
13	Function $f: \mathbb{R} \to \mathbb{R}$ , $f(x) = \frac{1}{x}$ is:
	X
	(a)one-one but not onto (b)onto but not one-one
	(c)function is not defined (d)neither one-one nor onto
14	Relation $R = \{(x, y) : x \le y^3 \text{ where } x, y \in \mathbb{R} \}$ is
	(a)Reflexive but not symmetric (b)Symmetric and transitive but not Reflexive
	(c)Reflexive and Symmetric (d)Neither reflexive nor symmetric nor transitive
15	Function defined by $f:\mathbb{Z} o\mathbb{W}$ , $f(x)=x^2$ is
	(a)one-one but not onto (b)onto but not one-one
	(c)one-one and onto (d)neither one-one nor onto

## Fill in the blanks(1 Mark)



### **4 Marks Questions**

- 1. Check reflexivity, symmetry and transitivity for the following relations:
  - (i)  $R = \{(x, y) : x y \text{ is an integer } \}$  (defined on the set of integers  $\mathbb{Z}$ )
  - (ii)  $R = \{(x, y) : |x y| \text{ is an integer } \}$  (defined on the set of integers  $\mathbb{Z}$ )
  - (iii)  $R = \{(x, y) : x y \text{ is divisible by } 3\}$  (defined on the set of integers  $\mathbb{Z}$ )
  - (iv)  $R = \{(x, y) : |x y| \text{ is divisible by } 6\}$  (defined on the set of integers  $\mathbb{Z}$ )
  - (v)  $R = \{(x, y) : x \le y^2 \text{ where } x, y \in \mathbb{R}\}$
  - (vi)  $R = \{(x, y): x \le y^3 \text{ where } x, y \in \mathbb{R}\}$
  - (vii)  $R = \{(l_1, l_2): line l_1 is parallel to the line l_2\}$  (Defined on the set of all lines L)
  - (viii)  $R = \{(l_1, l_2): line \ l_1 \ is \ parpendiculer \ to \ the \ line \ l_2\}$  (Defined on the set of all lines L in a plane)
- **2.** For the following functions  $f : R \rightarrow R$ :

(i) 
$$f(x) = \frac{3x+5}{2}$$
  
(ii)  $f(x) = \frac{2x-7}{4}$   
(iii)  $f(x) = \frac{3-2x}{4}$ 

(iv) 
$$f(x) = \frac{4-3x}{5}$$
  
(v)  $f(x) = \frac{6-5x}{7}$   
(vi)  $f(x) = \frac{5x+7}{6}$ 

show that these functions are one-one and onto.

## <u>UNIT – I</u> **Inverse Trigonometric Functions** Multiple Choice Questions(1 Marks Questions)

1	$\cos^{-1}\left(\cosrac{2\pi}{3} ight)$ is equal to	<b>)</b> :		
	(a) $\frac{\pi}{5}$	(b) $\frac{2\pi}{3}$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{3}$
2	$\sin^{-1}\left(\frac{1}{2}\right)$ is equal to :			
	(a)0	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{3}$
3	$\cos^{-1}(0)$ is equal to $:$			
	(a)0	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{3}$
4	$ an^{-1}(1)$ is equal to $:$			
	$(a)\frac{\pi}{4}$	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{3}$
5	If $y = \sin^{-1}(x)$ then $x$ b	elongs to the interval :		
	(a) $(0, \pi)$ (	<b>b)</b> (-1, 1)	(c) $\left[-1,1 ight]$ (d) $\left[0,\pi ight]$	
6	$\sin^{-1}\left(\sin\frac{\pi}{3}\right)$ is equal to	:		
	(a) $\frac{\pi}{5}$	(b) $\frac{2\pi}{3}$	(c) $\frac{\pi}{2}$	(d) $\frac{\pi}{3}$
7	If $\cos^{-1} x = y$ then x below	-		
0	(a)(0,1)	(b)(-1,1)	(c)[-1, 1]	(d)[0, 1]
8	Principal value of $\cos^{-1}$	<u> </u>	-	-
	(a)0	(b) $\frac{7\pi}{4}$	(c) $\frac{\pi}{4}$	$(d)\frac{\pi}{6}$
9	Range of function sec <sup>-1</sup>			
	(a) $[0,\pi]-\left\{rac{\pi}{2} ight\}$	<b>(b)</b> (0, π)	$(c)\left(-\frac{\pi}{2},\frac{\pi}{2}\right)-\{0\}$	(d) $[0,\pi]$
10	Domain of function cosed			
	(a)[-1, 1]	(b) $\mathbb{R}-(-1,1)$	( <b>c</b> )ℝ	(d)(-1,1)
11	Domain of the function ta	$an^{-1}$ is :		
	(a) $\left(-\frac{\pi}{2},\frac{\pi}{2}\right)$	(b) $\mathbb{R}-(-1,1)$	(c) <b>ℝ</b>	(d)(-1,1)
12	If $\tan^{-1} x = y$ , then y be	elongs to the interval :		
	(a) $\left(-\frac{\pi}{2},\frac{\pi}{2}\right)$	(b) $\mathbb{R}-(-1,1)$	(c) <b>ℝ</b>	(d) $(-1, 1)$

### **4 Marks Questions**

### 3. Find the values of : $7\cos^{-1}\left(\frac{1}{2}\right) + 12\tan^{-1}(1) - 4\sin^{-1}(1)$ (i)

- $5\cos^{-1}\left(\frac{\sqrt{3}}{2}\right) 3\tan^{-1}\left(\sqrt{3}\right) + 7\sin^{-1}\left(\frac{1}{2}\right)$ (ii) (iii)
- $5 \sec^{-1}\left(\sqrt{2}\right) + 8 \tan^{-1}(1) 3 \sin^{-1}\left(\sin\left(\frac{3\pi}{4}\right)\right)$   $2 \csc^{-1}(1) 5 \sec^{-1}\left(\frac{2}{\sqrt{3}}\right) + \sin^{-1}\left(\frac{1}{2}\right) 4 \cot^{-1}(\sqrt{3})$   $3 \csc^{-1}(1) + \sec^{-1}(2) 5 \sin^{-1}\left(\frac{\sqrt{3}}{2}\right) + 7 \cot^{-1}\left(\frac{1}{\sqrt{3}}\right)$ (iv)
- (v)

# <u>UNIT – II (Algebra)</u> <u>MATRICES& DETERMINANTS</u> <u>Multiple Choice Questions(1 Mark)</u>

1	If order o	of matrix $A$ is $2 imes$	3 and order of mat	rix $B$ is $3  imes$	5 then order	of matrix B	´A´ is :	
	(a)5	× 2	(b) $2 imes 5$	(c)	:) 5 × 3		(d) $3  imes 2$	
2		$\begin{vmatrix} l \\ c \end{vmatrix} = \begin{vmatrix} 2 & 0 \\ 8 & 4 \end{vmatrix}$ the					( 1)0	
2	(a)3		(b)2	-	:)4		(d)8	
5	If $\begin{bmatrix} 2x + \\ 5 \end{bmatrix}$	$\begin{bmatrix} y & 0 \\ x \end{bmatrix} = \begin{bmatrix} 5 & 0 \\ 5 & 3 \end{bmatrix}$	, then <b>y</b> is equal to:	-				
	(a)1		(b)3	(c)2		(d)-	-1	
4	: If A + B (a) 5		are matrices of ord (b) 5×3	ler 5×5 ther (c) 3			3×3	
5	lf A B = ( (a) 5		are matrices of orde (b) 5×2	er 2×5 and 5 (c) 2	-	-	r of A is :- 2×2	
6	If order o	of matrix $A$ is $2 imes$	3 and order of mat	rix $B$ is 3 $ imes$	5 then order	of matrix A	<i>B</i> is :	
	(a)5	× 2	(b) $2 imes 5$	(c)	c) 5 × 3		(d) $3 \times 2$	
7	If order o	of matrix $A$ is 4 $ imes$	3 and order of mat	rix $B$ is 3 $ imes$	< 5 then order	of matrix A	<i>B</i> is :	
	(a)5	× 4	(b) $4 imes 5$	(c)	:) 5 × 3		(d) $3  imes 4$	
8	If A is a (a)27		order $4 imes 4$ and $ A $ (b) $81$	= 3 then  A	A <i>dj</i> . (A)  is (c)9		(d)3	
9	If $A = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 5\\ -2 \end{bmatrix}$ then $ A $	is					
	(a)-9	(b)9		(c)1		(d)—1		
10			3  imes 3 and $ A  = 3$		A)  is			
	(a)81	(b)9		(c)27		(d)3		
			<u>FIII</u>	-ups(1 Ma	ark <u>)</u>			
	9)	If $A = [a_{ij}]_{2 \times 3}$	such that $a_{ij}=i+$	$j$ then $a_{11}$	1 =	_		
	10)	If $ A  = 5$ when	e $A$ is a matrix of or	rder $3 \times 3$	then $ adj.(A) $	)  =		
	11)	If matrix $A = \begin{bmatrix} 2\\ 1 \end{bmatrix}$	$\begin{bmatrix} 3\\5 \end{bmatrix}$ then $ A  =$		-			
	12)	If order of matrix	x $A$ is $3 imes 4$ then or	der of $A' =$				
	13)	If for a matrix ,A	$\mathbf{l}^{'}=oldsymbol{A}$ holds then $oldsymbol{A}$	is	m	atrix.		
	14)	If for a matrix ,	$\mathbf{l}^{'}=-A$ holds then	A is		matrix.		
	15)	If for any two ma	atrices Aand B, AB	= BA = I t	then these mat	trices are	of each other.	
	16)	matr	ix is symmetric as w	ell as skew-	-symmetric.			
	17)	If order of matrix	x $A$ is $3 imes 4$ and ord	ler of matrix	x $B$ is $4 imes 7$ the	en order of A	1 <i>B</i> is	
	18)	If order of matrix	x $A$ is $4 imes 5$ then nu	mber of ele	ements in A are	e		

# 2 Marks Questions5

1. If 
$$A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$$
, then verify  $A^2 - 7A - 2I = 0$ .

2. If 
$$A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$$
 show that  $A^2 - 5A - 14I = 0$ .  
3. If  $A = \begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix}$  and  $f(x) = x^2 - 4x + 1$  then find  $f(A)$ .  
4. If  $A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$  and  $f(x) = x^2 - 2x - 3$  then find  $f(A)$ .  
5. If  $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$  and  $A^2 - 8A = kI$  then find  $k$ .  
6. If  $A = \begin{bmatrix} 0 & 3 \\ -7 & 5 \end{bmatrix}$  then find  $k$  so that  $kA^2 = 5A - 21I$ .  
7. If  $X = \begin{bmatrix} 3 & 4 \\ 2 & -1 \end{bmatrix}$  and  $2X - Y = \begin{bmatrix} 5 & 10 \\ 3 & -5 \end{bmatrix}$  then find the matrix  $Y$ .  
8. If  $X - 2Y = \begin{bmatrix} 5 & 1 \\ 2 & 0 \end{bmatrix}$  and  $2X - Y = \begin{bmatrix} 4 & 9 \\ 1 & -3 \end{bmatrix}$  then find the matrices  $X$  and  $Y$ .  
9. Verify  $(AB)' = B'A'$  for the following matrices :

(i) 
$$A = \begin{bmatrix} 1 \\ 3 \\ 6 \end{bmatrix}$$
,  $B = \begin{bmatrix} 2 & 4 & 5 \end{bmatrix}$   
(ii)  $A = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} -2 & -1 & -4 \end{bmatrix}$   
(iii)  $A = \begin{bmatrix} 2 & 3 \\ 0 & 1 \end{bmatrix}$ ,  $B = \begin{bmatrix} 3 & 4 \\ 2 & 1 \end{bmatrix}$   
(iv)  $A = \begin{bmatrix} 4 & -2 \\ -1 & 3 \end{bmatrix}$ ,  $B = \begin{bmatrix} 2 & 7 \\ 5 & 0 \end{bmatrix}$   
(v)  $A = \begin{bmatrix} -1 & 3 & 0 \\ -7 & 2 & 8 \end{bmatrix}$ ,  $B = \begin{bmatrix} -5 & 0 \\ 0 & 3 \\ 1 & -8 \end{bmatrix}$   
(vi)  $A = \begin{bmatrix} 2 & 1 & 3 \\ 4 & 1 & 0 \end{bmatrix}$ ,  $B = \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 5 & 0 \end{bmatrix}$ 

- 10. Using determinants, show that following points are collinear :
  - (i) (11,7), (5,5) and (-1,3)
  - (ii) (3, 8), (-4, 2) and (10, 14)
  - (iii) (-2, 5), (-6, -7) and (-5, -4)
- 11. Find the value of x if (3, -2), (x, 2) and (8, 8) are collinear points.
- 12. Using determinants, find the value of k if the area of the triangle formed by the points

(-3, 6), (-4, 4) and (k, -2) is 12 sq. units.

- 13. If the area of triangle is 35 sq. units with vertices (2, -6), (5, 4) and (k, 4) then find the value of k.
- 14. Find the equation of the line passing from (3, 2) and (-4, -7) using determinants.

## 6/4 Marks Questions6

- 1. Solve the following system of linear equations by matrix method :
- (i) x y + 2z = 7, 3x + 4y 5z = -5, 2x y + 3z = 12

(ii) 
$$x + y + z = 6$$
,  $y + 3z = 11$ ,  $x - 2y + z = 0$   
(iii)  $3x + y + z = 10$ ,  $2x - y - z = 0$ ,  $x - y + 2z = 1$   
(iv)  $2x + 3y + 3z = 5$ ,  $x - 2y + z = -4$ ,  $3x - y - 2z = 3$   
(v)  $2x + 3y + 3z = 5$ ,  $x - 2y + z = -4$ ,  $3x - y - 2z = 3$   
(vi)  $x - y + 2z = 2$ ,  $3x + 4y - 5z = 2$ ,  $2x - y + 3z = 4$   
(vii)  $x + y - z = 3$ ,  $2x + 3y + z = 10$ ,  $3x - y - 7z = 1$   
(viii)  $x + y + z = 3$ ,  $5x - y - z = 3$ ,  $3x + 2y - 4z = 1$   
(ix)  $2x + 3y + 3z = 5$ ,  $x - 2y + z = -4$ ,  $3x - y - 2z = 3$   
(x)  $5x + y - z = -6$ ,  $2x - 3y + 4z = 3$ ,  $7x + y - 3z = -12$ 

2. Express the following matrices as a sum of a symmetric matrix and a skew-symmetric matrix :

(i) 
$$\begin{bmatrix} 2 & 0 & 3 \\ -1 & 4 & 8 \\ 7 & 2 & 9 \end{bmatrix}$$
 (ii)  $\begin{bmatrix} 3 & 6 & 2 \\ 0 & 7 & 8 \\ 5 & 1 & 9 \end{bmatrix}$   
(iii).  $\begin{bmatrix} 5 & 1 & 2 \\ -2 & 3 & 0 \\ 6 & 3 & 7 \end{bmatrix}$  (iv)  $\begin{bmatrix} 2 & 5 & 8 \\ -3 & 6 & 0 \\ 5 & 2 & 1 \end{bmatrix}$   
(v).  $\begin{bmatrix} 4 & 5 \\ 7 & 9 \end{bmatrix}$  (vi)  $\begin{bmatrix} 7 & -3 \\ 4 & 5 \end{bmatrix}$ 

	Δ	Continuity 8	<u>NIT – III</u> & Differentiabili e Questions (1 Ma	
1	$lff(x) = \begin{cases} kx + 1, & x \le 5\\ 3x - 5, & x > 5 \end{cases}$			
	(a) <del>5</del>	(b) <u>5</u>	(c) $\frac{5}{3}$	(d) $\frac{3}{5}$
2	If $f(x) = \begin{cases} kx^2, & x \le 2\\ 3, & x > 2 \end{cases}$ is	continuous then	value of k is :	
	$(a)\frac{2}{3}$	(b) $\frac{4}{3}$	(c) $\frac{3}{2}$	(d) $\frac{3}{4}$
3	$lff(x) = \begin{cases} mx - 1, & x \le 5\\ 3x - 5, & x > 5 \end{cases}$	is continuous th	nen value of $m$ is :	
	(a) $\frac{11}{5}$	(b) $\frac{5}{11}$	(c) $\frac{5}{2}$	(d) $\frac{3}{5}$
4	$lff(x) = \begin{cases} mx^2, & x \le 5\\ 6x - 5, & x > 5 \end{cases}$	is continuous the	en value of $m$ is :	
-	(a)- 1	(b)4	(c)3	(d)1
5	$lff(x) = \begin{cases} \frac{\sin 2x}{3x} , & x \neq 0\\ m-1, & x = 0 \end{cases}$	is continuous the	en value of $m$ is :	
	(a)2/3	(b)3/2	(c)3/5	(d)5/3
6	$lff(x) = \begin{cases} kx + 1, & x \le 5\\ 3x + 5, & x > 5 \end{cases}$	is continuous the	en value of <i>k</i> is :	
_	$(a)\frac{19}{5}$	(b) $\frac{5}{2}$	(c) $\frac{5}{2}$	(d) $\frac{3}{5}$
7	$lff(x) = \begin{cases} kx - 1, & x \le 5\\ 3x + 5, & x > 5 \end{cases}$	is continuous the		
-	(a) $\frac{21}{5}$ (b) $\frac{5}{19}$	(c) $\frac{5}{21}$	(d) $\frac{19}{5}$	
8	If $f(x) = \begin{cases} \frac{\sin 7x}{3x}, x \neq 0\\ m, x = 0 \end{cases}$ is	continuous at $x =$	= 0 then value of $m$ is	
	(a) $\frac{3}{7}$ (b) $\frac{4}{7}$		c) <sup>7</sup> / <sub>4</sub>	$(d)\frac{7}{3}$
9	If $y = \log\left[x + \sqrt{x^2 + 1}\right]$	ил	•	5
	(a) $\sqrt{x^2 + 1}$ (b) $\frac{1}{\sqrt{x^2 + 1}}$	(c) $\frac{x}{\sqrt{x^2+1}}$ (d	$\left(\frac{1}{x+\sqrt{x^2+1}}\right)$	
10	If $f(x) = \begin{cases} \frac{x^3 - 8}{x - 2}, & x \neq 2\\ k, & x = 2 \end{cases}$ is	s continuous at $x$	= 2 then value of <i>k</i> is	
	(a)8 (b)2 (c)6		(d)12	
11	$\frac{d}{dx}$ {tan <sup>-1</sup> ( $e^x$ )}is equal to $e^x$			. 1
12	(a) $e^x \tan^{-1} e^x$ (b) $\frac{e^x}{1+e^2}$		c) 0	(d) $e^x \sec^{-1} x$
12	If $y = \sin x$ then at $x = \frac{\pi}{2}$ (a)-1 (b)		(c) 0	(d) $\frac{1}{2}$
13	If $x = 2at$ , $y = at^2$ then			(a) <sub>2</sub>
	(a)2 (b)2 <i>a</i>	(c)2 <i>at</i>	(d) <i>t</i>	
14	If $y = \cos^{-1}(e^x)$ then $\frac{dy}{dx}$		a <sup>x</sup>	a <sup>x</sup>
	(a) $e^x \sin^{-1}(e^x)$ (b		(c) $\frac{-e}{\sqrt{1-e^{2x}}}$	(d) $\frac{e^x}{\sqrt{1-e^{2x}}}$
15	If $y = \sin^{-1}(e^x)$ then $\frac{dy}{dx}$		$-\rho^{\chi}$	ex ex
16	(a) $e^x \sin^{-1}(e^x)$		) (c) $\frac{-e^x}{\sqrt{1-e^{2x}}}$	(d) $\frac{e^{x}}{\sqrt{1-e^{2x}}}$
16	$\frac{d}{dx} \{ \cot^{-1}(e^x) \} \text{ is equal to } :$	r	$e^{x}$	(n r _1
	(a) $e^x \tan^{-1} e^x$	(b) $\frac{1}{1+e^{2x}}$	(c) $\frac{-e^x}{1+e^{2x}}$	(d) $e^x \sec^{-1} x$

17
 If 
$$y = x^2$$
 then  $y_1(5)$  is equal to :

 (a)10
 (b)25
 (c)32

 18
 If  $y = \log(\sin x)$  then at  $x = \frac{\pi}{4}, \frac{dy}{dx}$  is

 (a)0
 (b)-1
 (c)1

 19
 If  $y = e^{\log x}$  then  $\frac{dy}{dx}$  is

 (a)log  $x - x$ 
 (b) $xe^{\log x}$ 
 (c)1

 20
 If  $y = \log(\sec x)$  then  $\frac{dy}{dx}$  at  $x = \frac{\pi}{4}$  is

 (a)1
 (b)-1
 (c)0

 (d)10

### **2 Marks Questions**

- **1.** Find the relation between *a* and *b* if  $f(x) = \begin{cases} ax + 1, & if x \le 3 \\ bx + 3, & if x > 3 \end{cases}$  is a continuous at = 3.
- 2. Find the values of a and b if the following function is continuous :

$$f(x) = \begin{cases} 5 & , & if \ x \le 2 \\ ax + b & , & if \ 2 < x < 10 \\ 21 & , & if \ x \ge 10 \end{cases}$$

**3.** Find  $\frac{dy}{dx}$  for the following parametric functions :

(i) 
$$x = a \cos^2 \theta$$
,  $y = b \sin^2 \theta$   
(ii)  $x = a(\theta - \sin \theta)$ ,  $y = b(1 + \cos \theta)$ 

- (iii)  $x = a(\theta + \sin \theta)$ ,  $y = b(1 + \cos \theta)$
- (iv)  $x^2 + y^2 + 2xy = 23$
- (v)  $y = \sin^{-1}\left(\frac{2x}{1+x^2}\right)$

(vi) 
$$y = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$$

(vii)  $x^3 + 3x^2y + 3xy^2 + y^3 = 81$ 

#### **4Marks Questions**

1) If  $x = 2\cos\theta - \cos 2\theta$ ,  $y = 2\sin\theta - \sin 2\theta$  then find  $\frac{dy}{dx}$  at  $\theta = \frac{\pi}{2}$ .

2) If 
$$x = \frac{1-t^2}{1+t^2}$$
,  $y = \frac{2t}{1+t^2}$  then prove that  $\frac{dy}{dx} + \frac{x}{y} = 0$ .

- 3) Differentiate the following w.r.t. :
  - (i)  $x^{\sin x} + (\sin x)^x$  (ii)  $x^{\log x} + (\log x)^x$  (iii)  $x^{\tan x} + (\tan x)^x$
  - (iv)  $x^{\cos x} + (\sin x)^{\tan x}$  (v)  $x^x + (\sin x)^x$  (vi)  $x^{\sin^{-1}x} + (\sin^{-1}x)^x$
- 4) Solve the following :
- (i) If  $(\sin x)^y = (\sin y)^x$ , find  $\frac{dy}{dx}$ .
- (ii) If  $(\sin x)^y = (\cos y)^x$ , find  $\frac{dy}{dx}$ .

(iii) If 
$$y = x^y$$
 show that  $\frac{dy}{dx} = \frac{y^2}{x(1-y\log x)}$ .

- (iv) If  $x^y + y^x = \log a$  , find  $\frac{dy}{dx}$ .
- 5) If  $y = \sin^{-1} x$  then show that  $(1 x^2) \frac{d^2 y}{dx^2} x \frac{dy}{dx} = 0$ .
- 6) If  $y = (\sin^{-1} x)^2$  then prove that  $(1 x^2) \frac{d^2 y}{dx^2} x \frac{dy}{dx} = 2$ .
- 7) If  $y = (\tan^{-1} x)^2$  then show that  $(1 + x^2)^2 y_2 + 2x(1 + x^2)y_1 2 = 0$ .
- 8) If  $y = \log(x + \sqrt{x^2 + 1})$  then show that  $(x^2 + 1)\frac{d^2y}{dx^2} + x\frac{dy}{dx} = 0$ .
- 9) If  $y = e^{m \sin^{-1} x}$  then show that  $(1 x^2)y_2 xy_1 m^2 y = 0$ .
- 10) If  $y = e^{m \tan^{-1} x}$  prove that

(i)
$$(1+x^2)\frac{d^2y}{dx^2}+(2x-m)\frac{dy}{dx}=0$$
 (ii)  $(1+x^2)^2y_2+2x(1+x^2)y_1-m^2y=0$ .

# <u>UNIT – III</u> Applications of Derivatives

### **Multiple Choice Questions (1 Marks)**

1 Rate of change of perimeter of a square with respect to its side is : (d)3 (a)2 (b)1 (c)4 2 Radius of a circle is increasing at the rate of 2 m/s. Rate of change of its circumference is : (c) $2\pi m/s$ (a) $4\pi m/s$ (b)2 m/s(d)4 m/s3 Radius of a sphere is increasing at the rate of 5 m/s. Rate of change of its surface area, when radius is 4 m, is (b)  $160\pi m^2/s$ (c)  $32\pi m^2/s$ (d)  $80\pi m^2/s$ (a)  $120\pi m^2/s$ 4  $f(x) = \sin x$  is strictly decreasing in the interval :  $(c)\left(0,\frac{\pi}{2}\right)$  $(d)\left(\frac{\pi}{2},\frac{3\pi}{2}\right)$  $(b)\left(\pi,\frac{3\pi}{2}\right)$  $(a)\left(\frac{\pi}{2},\pi\right)$ 5  $f(x) = \cos x$  is strictly increasing in the interval :  $(c)\left(0,\frac{\pi}{2}\right)$  $(b)\left(\pi,\frac{3\pi}{2}\right)$  $(d)\left(\frac{\pi}{2},\frac{3\pi}{2}\right)$  $(a)\left(\frac{\pi}{2},\pi\right)$ 6  $f(x) = x^2$  strictly increases on : **(b)**(−∞, **0**) **(c)**(−7, −3) (a)(0,∞)  $(d)(-\infty, -3)$ 7 If f is differentiable at critical points then the value of derivative of f at critical point is : (a)1 (b) - 1(c)0 (d)2 8 On the curve y = f(x) if f'(a) = 0 then x = a is called a (a)Practical point on the curve (b)Critical point on the curve (c)Maximum point on the curve (d)Minimum point on the curve 9 On the curve y = f(x) if f'(a) = 0 and f''(a) < 0 then x = a is point of (b)Minima (d)infinity (a)Maxima (c)Inflexion 10 On the curve y = f(x) if f'(a) = 0 and f''(a) > 0 then x = a is point of (a)Maxima (b)Minima (c)Inflexion (d)infinity

### **True/False**

- 1) Function f decreases where f'(x) > 0.
- **2)** Function f decreases where f'(x) < 0.
- 3)  $f(x) = \sin x$  is strictly decreasing function in  $\left|0, \frac{\pi}{2}\right|$ .
- 4) The value of function f is maximum at a if f'(a) = 0 and f''(a) < 0.
- 5) Logarithmic function  $f(x) = \log x$  is a strictly increasing function.
- 6) Velocity of a moving particle cannot be expressed as derivative of displacement function of the particle.
- 7) The value of function f is maximum or minimum at x = a if f'(a) = 0 and  $f''(a) \neq 0$
- 8) The value of function f is minimum at a if f'(a) = 0 and f''(a) < 0.
- 9) When f'(a) = 0 then x = a is called a critical point on the curve y = f(x)
- 10) If a given cylindrical bucket is being filled with water with a given rate then we can evaluate the rate of change of the height of water cylinder inside the bucket.

### **2 Marks Questions**

- 1. The volume of spherical balloon is increasing at the rate of 25 c.c./s . Find the rate of change of its surface area at the instant when its radius is 5 cm.
- 2. The side of square sheet is increasing at the rate of 3 cm/s. At what rate is the area increasing when the side is 10 cm long?
- 3. The side of square sheet is increasing at the rate of 5 cm/s. At what rate is the perimeter increasing when the side is 7 cm long?

- 4. The radius of spherical soap bubble is increasing at the rate of 0.2 cm/s. Find the rate of change of its volume when its radius is 4 cm.
- 5. The radius of spherical soap bubble is increasing at the rate of 0.8 cm/s. Find the rate of change of its surface area when the radius is 5 cm.
- 6. The edge of a cube is decreasing at the rate of 2 cm/s. Find the rate of change of its volume when the length of edge of the cube is 5 cm.
- 7. The edge of a cube is decreasing at the rate of 2 cm/s. Find the rate of change of its surface area when the length of edge is 6 cm.
- 8. Find the critical points of the following functions :

(a) $f(x) = x^3 + 2x^2 - 1$	(b) $f(x) = 30 - 24x + 15x^2 - 2x^3$	(c) $f(x) = 20 - 12x + 9x^2 - 2x^3$
$(d)f(x) = 17 - 18x + 12x^2 - 2x^3$	(e) $f(x) = 20 - 9x + 6x^2 - x^3$	(f) $f(x) = 6 + 12x + 3x^2 - 2x^3$
(g) $f(x) = 2x^3 - 15x^2 + 36x + 1$	(h) $f(x) = x^3 - 6x^2 + 9x + 8$	(i) $f(x) = 2x^3 - 12x^2 + 18x + 5$

9. Determine the intervals in which the following functions are increasing or decreasing :

(a) $f(x) = x^3 + 2x^2 - 1$	(b) $f(x) = 30 - 24x + 15x^2 - 2x^3$	(c) $f(x) = 20 - 12x + 9x^2 - 2x^3$
(d) $f(x) = 17 - 18x + 12x^2 - 2x^3$	(e) $f(x) = 20 - 9x + 6x^2 - x^3$	(f) $f(x) = 6 + 12x + 3x^2 - 2x^3$
$(g)f(x) = 2x^3 - 15x^2 + 36x + 1$	(h) $f(x) = x^3 - 6x^2 + 9x + 8$	(i) $f(x) = 2x^3 - 12x^2 + 18x + 5$

### **6 Marks Questions**

- 1. Find the volume of the biggest right circular cone which is inscribed in a sphere of radius 9cm.
- 2. Prove that the height of a right circular cylinder of maximum volume, which is inscribed in a sphere of radius *R*, is  $\frac{2R}{\sqrt{3}}$ .
- 3. Show that of all the rectangles inscribed in a given fixed circle, the square has the maximum area.
- 4. A wire of length 25 m is to be cut into two pieces. One of the pieces is to be made into a square and the other into a circle. What could be the lengths of the two pieces so that the combined area of the square and circle is minimum?
- 5. A wire of length 20 m is to be cut into two pieces. One of the pieces is to be made into a square and the other into an equilateral triangle. What could be the lengths of the two pieces so that the combined area of the square and equilateral triangle is minimum?
- 6. Prove that the perimeter of a right angled triangle of given hypotenuse equal to 5 cm is maximum when the triangle is isosceles.
- 7. Of all rectangles with perimeter 40 cm find the one having maximum area. Also find the area.
- 8. Find the volume of the largest cylinder that can be inscribed in a sphere of radius R.
- 9. Find the volume of largest cone that can be inscribed in a sphere of radius R.
- 10. Show that height of the cylinder of maximum volume that can be inscribed in a sphere of 30 cm is  $\frac{60}{\sqrt{3}}$  cm.
- 11. A window is in the form of rectangle surmounted by a semi-circle opening. If the perimeter of window is 10 cm, find the dimensions of the window so as to admit maximum possible light through the whole opening.
- 12. Show that the height of a closed cylinder of given volume and least surface area is equal to its diameter.

## UNIT – III INTEGRALS Fill in the Blanks(1 Marks)

1.  $\int_0^3 dx =$ \_\_\_\_\_ 2.  $\int \sec^2 x \, dx =$ \_\_\_\_\_  $\int_0^3 3x^2 dx = \underline{\qquad}$ 3. 4.  $\int_0^5 2x dx =$ \_\_\_\_\_ Integration is \_\_\_\_\_ process of differentiation. 5.  $\int_{-a}^{a} f(x) \, dx = 0 \text{ if } f \text{ is } \qquad \text{function.}$ 6.  $\int \frac{dx}{1+x^2} = \underline{\qquad}$ 7.  $\int_0^{\pi/2} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx = \underline{\qquad}$ 8.  $\int \frac{1}{x+3} dx = \underline{\qquad}$  $\int \sec x \tan x \, dx = \underline{\qquad}$ 9. 10. Multiple Choice Questions(1 Marks) 1  $\int_0^{\pi/2} \frac{\sin^{1/2} x}{\sin^{1/2} x + \cos^{1/2} x} dx$  is equal to : (c)  $\frac{\pi}{3}$ (d)  $\frac{\pi}{4}$ (b)  $\frac{\pi}{2}$ 2  $\int_0^{\pi/2} \frac{\sin^{3/2} x}{\sin^{3/2} x + \cos^{3/2} x} dx$  is equal to : (c)  $\frac{\pi}{3}$ (d)  $\frac{\pi}{4}$ (a)0 (b)  $\frac{\pi}{2}$ **3**  $\int \frac{dx}{2x+3}$  equals: (a) $\log |2x+3| + c$  (b) $\log |2x-3| + c$  (c) $\frac{\log |2x+3|}{3} + c$  (d) $\frac{\log |2x+3|}{2} + c$ 4  $\int \frac{dx}{2x-5}$  equals:  $(\mathsf{d})^{\frac{\log|2x-5|}{2}} + c$ (b) $\log |2x+5| + c$  (c) $\frac{\log |2x-5|}{5} + c$ (a) $\log |2x - 5| + c$ 5  $\int_{-1}^{1} x^3 \cos x \, dx$  equals: (a)0 (b)1/4 (c)π (d)none of these 6  $\int_0^{\pi/2} \frac{\sin^{1/2} x}{\sin^{1/2} x + \cos^{1/2} x} dx$  is equal to : (c)  $\frac{\pi}{3}$ (b)  $\frac{\pi}{2}$ (d)  $\frac{\pi}{4}$ (a)0 7  $\int_{-2}^{2} x^3 dx$  is equal to : (d)  $\frac{\pi}{4}$ (a)0 (b)4 (c)16/3 8  $\int_{-1}^{1} x \sin^2 x \, dx$  is equal to  $(b)\frac{1}{2}$  $(c)^{\frac{1}{2}}$ (a)0 (d) - 19  $\int_0^1 \frac{dx}{1+x^2}$  is (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{2}$  $(c)\frac{\pi}{4}$  $(d)\frac{\pi}{6}$ 

10  $\int_{\pi/6}^{\pi/3} \frac{\cos^4 x}{\sin^4 x + \cos^4 x} dx$  is equal to

(a) $\frac{\pi}{4}$  (b) $\frac{\pi}{6}$ 

$$(d)\frac{\pi}{2}$$

## **2 Marks Questions**

 $(c)\frac{\pi}{12}$ 

- 1. Evaluate the following :
  - $(a) \int \frac{(x-4)^3}{x^2} dx \qquad (b) \int \frac{dx}{1-\sin x} \qquad (c) \int \frac{dx}{1+\cos x} \qquad (d) \int \frac{dx}{1+\sin x}$   $(e) \int \frac{dx}{1-\cos x} \qquad (f) \int \frac{e^x 1}{e^x + 1} dx \qquad (g) \int \frac{(\tan^{-1} x)^2}{1+x^2} dx \qquad (h) \int \frac{\sec^2(2\tan^{-1} x)}{1+x^2} dx$   $(i) \int \frac{\sin(\tan^{-1} x)}{1+x^2} dx \qquad (j) \int \frac{dx}{x^2 + 8x 9} \qquad (k) \int \frac{dx}{\sqrt{x^2 5x + 7}} \qquad (l) \int \frac{dx}{\sqrt{x^2 + 4x + 7}}$   $(m) \int \frac{dx}{x^2 + 6x + 5} \qquad (n) \int \frac{dx}{x^2 6x + 18} \qquad (o) \int x\sqrt{x + 2} dx \qquad (p) \int \frac{3 2\sin x}{\cos^2 x} dx$
- 2. Compute the following :

(a) 
$$\int \frac{\log x}{x} dx$$
 (b)  $\int \frac{e^{\tan^{-1} x}}{1+x^2} dx$  (c)  $\int \frac{2x}{1+x^2} dx$  (d)  $\int \frac{x^2}{1+x^3} dx$   
(e)  $\int \frac{6x-8}{3x^2-8x+5} dx$  (f)  $\int \frac{2x+9}{x^2+9x+20} dx$  (g)  $\int e^x \left( \tan^{-1} x + \frac{1}{1+x^2} \right) dx$ 

## **4 Marks Questions**

3. Integrate the following : (a) $\sin^2 x \cos^3 x$ (b) $\cos^2 x \sin^3 x$ (c) $\frac{1}{1-\cot x}$ 

$$(\mathsf{d})\frac{1}{1+\cot x}(\mathsf{e})\frac{1}{1-\tan x} \qquad (\mathsf{f})\frac{1}{1+\tan x}$$

- 4. Evaluate the following integrals : (a)  $\int \frac{1-\tan x}{1+\tan x} dx$  (b)  $\int \frac{1+\tan x}{1-\tan x} dx$
- 5. Integrate the following functions: (a)  $x \sec^2 x$ (b)  $x^2 e^x$ (c)  $x \cos 3x$ (d)  $x \sin x$
- 7. Integrate the following functions :(a)  $e^x \sin 2x$ (b)  $e^{3x} \cos 5x$ (c)  $e^x$

(c) $e^x(\cot x + \log \sin x)$ 

8. Integrate the following functions :

(a) 
$$\frac{1}{(x+1)(x+2)(x+3)}$$
 (b)  $\frac{1}{x(x-1)(x-2)}$  (c)  $\frac{1}{x^3-1}$  (d)  $\frac{1}{(1-x)(1+x^2)}$   
(e)  $\frac{x}{(x-2)(x^2+4)}$  (f)  $\frac{1}{x(x^2+2)}$ 

9. Integrate the following functions :

(a) 
$$\frac{2x}{\sqrt{(x+1)(x-2)}}$$
 (b)  $\frac{4x+5}{\sqrt{x^2+x-3}}$  (c)  $\frac{3x+5}{\sqrt{x^2-8x+7}}$ 

### **12** Evaluate the following integrals :

(a) 
$$\int_{0}^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$$
  
(b)  $\int_{0}^{\pi/2} \frac{1}{1 + \sqrt{\cot x}} dx$   
(c)  $\int_{0}^{\pi/2} \frac{\sqrt{\cot x}}{\sqrt{\tan x} + \sqrt{\cot x}} dx$   
(e)  $\int_{0}^{1} |x - 5| dx$   
(f)  $\int_{-6}^{6} |x + 2| dx$   
(h)  $\int_{0}^{\pi/2} \log(\cos x) dx$ 

## 6 Marks Questions

### **Evaluate the following :**

1. 
$$\int \frac{x^2 + 1}{x^4 + 1} dx$$
  
2.  $\int \frac{x^2}{x^4 + 1} dx$ 

$$3. \quad \int \frac{1}{x^4+1} dx$$

 $4. \quad \int_0^{\pi/2} \log \cos x \, dx$ 

$$5. \quad \int \frac{2x}{(x^2+1)(x^2+4)} dx$$

$$6. \quad \int \frac{1}{x^3 - 1} dx$$

- 7.  $\int (\sqrt{\cot x} + \sqrt{\tan x}) dx$
- $8. \quad \int_0^\pi \frac{x dx}{a^2 \cos^2 x + b^2 \sin^2 x}$

# <u>UNIT – III</u> <u>APPLICATIONS OF INTEGRALS</u> <u>2 Marks Questions</u>

1. Using integration, find the area of the circle :

- (i)  $x^2 + y^2 = 4$  (ii)  $x^2 + y^2 = 9$ (iii)  $\frac{x^2}{9} + \frac{y^2}{4} = 1$  (iv)  $\frac{x^2}{9} + \frac{y^2}{25} = 1$ (v)  $\frac{x^2}{16} + \frac{y^2}{26} = 1$  (vi)  $\frac{x^2}{25} + \frac{y^2}{16} = 1$
- 2. Find the area of the region bounded by  $x^2 + y^2 = 16$ , y = x in the first quadrant.
- 3. Find the area of the region bounded by  $x^2 + y^2 = 25$ , y = 2x in the first quadrant
- 4. Draw a rough sketch to indicate the region bounded between the curve  $y^2 = 4x$ , x = 3. Also find the area of this region.
- 5. Find the area of the region bounded by the curves  $y^2 = 8x$ , x = 1, x = 5 in the first quadrant.
- 6. Find the area bounded by the three line y = x, x = 2 and x = 5 in the first quadrant.
- 7. Find the area bounded by the parabola  $y^2 = 16x$  and its latusrectum.

# <u>UNIT – III</u> <u>DIFFERENTIAL EQUATIONS</u> <u>Multiple Choice Questions(1 Marks)</u>

1	Integrati	ting factor of differential equation $\frac{dy}{dx} - \frac{y}{x} = 2$	2x is:	
	(a) $\frac{1}{r}$	1	c) $\frac{1}{n^2}$	(d)1
2	л	of differential equation $\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^3 + y = 0$ i	<i>x</i> -	
	(a) 3	3 (b) 2	(c) 0	(d)1
3	Differen	ntial equation for the family of the curves $y^2$ =	= kx is:	(*)-
	$(a)\frac{dy}{dx} = 0$	$0  (b)y + 2x\frac{dy}{dx} = 0$	(c) $y - 2x \frac{dy}{dx} = 0$	$(d)y\frac{dy}{dx} = 1$
4	Integrati	ting factor of differential equation $\frac{dy}{dx} + \frac{y}{x} = 2x$	x is:	
	(a) $\frac{1}{x}$	(b) $x^2$	(c) $\frac{1}{x^2}$	(d) <i>x</i>
5	Integrati	ting factor of differential equation $\frac{dy}{dx} + \frac{2y}{x} = 2$	2 <i>x</i> is:	
	$(a)\frac{1}{x}$	(b) $x^2$	(c) $\frac{1}{x^2}$	(d) <i>x</i>
6	Integrati	ting factor of differential equation $\frac{dy}{dx} + y \sec \theta$	x = 2x is:	
	(a)sec x	$x + \tan x$ (b) sec $x \tan x$	(c) $e^{\sec x}$	(d) $e^{\sec x + \tan x}$
7	Integrati	ting factor of differential equation $\frac{dy}{dx} + y = 2$	2 <i>x</i> is:	
	(a) $\frac{1}{x}$	(b) $x$ (c) $e^x$	(d) $e^{-x}$	
8	Order of	of differential equation $rac{d^3y}{dx^3} - 4\left(rac{d^2y}{dx^2} ight)^4 + y = 0$	) is	
	(a)3	(b)4 $(dx^3)(dx^2)$	(c)1	(d)0
9		mber of arbitrary constants in the general solu		ation of second order are
10	(a)1	(b)2 (c)3 $d^{3}y d^{2}y (dy)^{4}$		
10		of the differential equation $\frac{d^3y}{dx^3} - \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^4$		
	(a)1	(b)2 (c)3	(d)	)4
		<u>Fill Up</u>	s(1 Marks)	
	19)	Order of the differential equation $\frac{d^2y}{dx^2} - \left(\frac{d}{dx}\right)^2$	$\left(\frac{y}{y}\right)^3 + y = 0$ is	
	20)	Degree of the differential equation $\frac{d^2y}{dx^2} - \left(\frac{d^2y}{dx^2} - \frac{d^2y}{dx^2}\right)$		
	21)	Integrating factor of differential equation $\frac{d}{d}$		
	22)	Order and degree (if defined) of a differenti		integers.
	23)	Integrating factor of $\frac{dx}{dy} + Px = Q$ is		
	24)	(x+y)dy - (x-2y)dx = 0 is a		
	25)	substitution is applied to solve a	•	•
	26)	There arenumber of arbitrary con of order 3.	istants in the general solu	ution of differential equation
	27)	Differential equation representing the famil	ly of curve $y=mx+c$ is	s given by
	28)	After correct substitution, a homogeneous on differential equation.	differential equation beco	omes type of

# 4 Marks Questions

Solve the following differential equations :

1) 
$$\frac{dy}{dx} = \log x$$
  
2)  $\frac{dy}{dx} + \frac{1+y^2}{y} = 0$   
3)  $\frac{dy}{dx} = \sin^2 y$   
4)  $\frac{dy}{dx} = e^y \sin x$   
5)  $\log \frac{dy}{dx} = ax + by$   
6)  $x^2(y+1)dx + y^2(x-1)dy = 0$   
7)  $\sec^2 x \tan y \, dx - \sec^2 y \tan x \, dy = 0$   
8)  $xdy + ydx = xydx; y(1) = 1$   
9)  $x(xdy - ydx) = ydx; y(1) = 1$   
10)  $\frac{dy}{dx} = y \tan x; y(0) = 1$   
11)  $\frac{dy}{dx} = y \sin 2x; y(0) = 1$   
12)  $(x^2 + xy)dy + (3xy + y^2)dx = 0$   
13)  $(y^2 - x^2)dy - 3xydx = 0$   
14)  $2xydx + (x^2 + 2y^2)dy = 0$   
15)  $x^2dy - (x^2 + xy + y^2)dx = 0$   
16)  $\cos(\frac{dy}{dx}) = \frac{1}{9}; y(0) = 2$   
17)  $(x^2 + y^2)dx + 2xydy = 0$   
18)  $(x^2 - 2y^2)dx + xydy = 0$ 

19) 
$$\frac{dy}{dx} + \frac{y}{x} = e^{x}$$
  
20)  $\frac{dy}{dx} - 4y = e^{2x}$   
21)  $x\frac{dy}{dx} + y = x^{3}$   
22)  $\frac{dy}{dx} + 2y = \sin 5x$   
23)  $\frac{dy}{dx} + 3y = \cos 2x$   
24)  $x\frac{dy}{dx} + y = x \log x$   
25)  $(1 + x^{2})\frac{dy}{dx} + y = \tan^{-1} x$   
26)  $\frac{dy}{dx} = 2x + y; y(0) = 0$   
27)  $\frac{dy}{dx} = 4x + y; y(0) = 1$   
28)  $x\frac{dy}{dx} + y = x^{3}; y(2) = 1$   
29)  $xy' - y = \log x; y(1) = 0$   
30)  $x \log x\frac{dy}{dx} + y = \frac{2}{x}\log x$   
31)  $\frac{dy}{dx} = \frac{1-\cos x}{1+\cos x}$   
32)  $(1 + x^{2})dy + 2xydx = \cot x dx$   
33)  $x\frac{dy}{dx} + 2y = x^{2}\log x$   
34)  $x^{2}dy - (3x^{2} + xy + y^{2})dx = 0; y(1) = 1$ .

# <u>UNIT – IV</u>

# **Vector Algebra**

# Multiple Choice Questions(1 Mark)

		marcip		
1	If $\vec{a}$ . $\vec{b} =  \vec{a} \times$	$ec{b} $ then angle between ve	ector $ec{a}$ and vector $ec{b}$ is :	
	(a) $\frac{\pi}{2}$	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{4}$	(d) $\frac{\pi}{3}$
2	Magnitude o	f the vector $\frac{1}{\sqrt{3}} \stackrel{\wedge}{i} + \frac{1}{\sqrt{3}} \stackrel{\wedge}{j}$	$+\frac{1}{\sqrt{3}}\overset{\wedge}{k}$ is :	
	(a)—1	(b)1	(c)0	$(d)\frac{1}{3}$
3	If $\sqrt{3}\vec{a}$ . $\vec{b} =  \vec{a} $	$ec{a}  imes ec{b} $ then angle betwee	n vector $ec{a}$ and vector $ec{b}$ is :	Ū.
	(a) $\frac{\pi}{2}$	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{4}$	(d) $\frac{\pi}{3}$
4	$ \mathbf{f}\vec{a}.\vec{b}=\sqrt{3} \vec{a}$	$ec{a} imesec{b}ert$ then angle betwee	n vector $ec{a}$ and vector $ec{b}$ is :	
	(a) $\frac{\pi}{2}$	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{4}$	(d) $\frac{\pi}{3}$
5	If $\vec{a}$ . $\vec{b} = 0$ the	en angle between vector $\overline{a}$	$ec{t}$ and vector $ec{b}$ is :	
	(a) $\frac{\pi}{2}$	(b) $\frac{\pi}{6}$	(c) $\frac{\pi}{4}$	(d) $\frac{\pi}{3}$
6	Name of the	inequality $\left  \vec{a} \cdot \vec{b} \right  \leq \left  \vec{a} \right  \left  \vec{b} \right $	is :	
	• • •	hwartz Inequality(b)Trian quality (d)Lagrange's Inc		
7	Magnitude o	f vector $\vec{a} = 3 i + j + j$	<i>k</i> is :	
	(a) 3	(b) $\sqrt{10}$	(c) $\sqrt{11}$	(d) $\sqrt{12}$
8	Projection of	$\vec{a} = 3 \vec{i} + \vec{j} + \vec{k}$ on $\vec{b}$	$\stackrel{\wedge}{=} \stackrel{\wedge}{i} \stackrel{\wedge}{-} \stackrel{\wedge}{2} \stackrel{j}{j} \stackrel{k}{-} k$ is :	
	(a) $\frac{2}{\sqrt{6}}$	(b)0	(c) $\frac{1}{\sqrt{6}}$	(d) $\sqrt{6}$
9		zero vector then $ \vec{a} \times \vec{a} $	-	
	(a)  <b>α</b>   ∧	(b) $ \vec{a} ^2$	(c)1 ∧ ∧	(d)0
10	If $\vec{a} = i + 2$	$2j - 3k$ and $\vec{b} = 2i$ -	$-2j - k$ then $\vec{a}$ . $\vec{b}$ is equal to	
	(a)1 (b)0	(c)—1	(d)3	

# 2 Marks Questions

- 1. Adjacent sides of a parallelogram are given by  $\hat{i} + 2\hat{j} \hat{k}$  and  $3\hat{i} \hat{j} + 5\hat{k}$ . Find a unit vector along a diagonal of the parallelogram.
- 2. Adjacent sides of a parallelogram are given by  $6\hat{i} \hat{j} + 5\hat{k}$  and  $\hat{i} + 5\hat{j} 2\hat{k}$ . Find the area of parallelogram.

- 3. Find the area of triangle whose sides are given by the vectors  $\hat{t} 2\hat{j} + \hat{k}$  and  $4\hat{t} + \hat{j} 7\hat{k}$ .
- 4. Find the value of p if the vectors  $p\hat{i} + \hat{j} + 4\hat{k}$  and  $2\hat{i} \hat{j} + 3\hat{k}$  are perpendicular to each other.
- 5. Find a vector of magnitude 8units along  $\vec{a} = 2\hat{i} 4\hat{j} + \hat{k}$
- 6. Find a unit vector along  $\vec{a} = 5\hat{\imath} + 3\hat{\jmath} 4\hat{k}$
- 7. If  $\vec{a} = 2\hat{\imath} 4\hat{\jmath} + \hat{k}$ ,  $\vec{b} = 3\hat{\imath} \hat{\jmath} 5\hat{k}$  then find  $|\vec{a} \times \vec{b}|$ .
- 8. Find the projection of  $\vec{a} = 2\hat{\imath} 4\hat{\jmath} + \hat{k}$  on  $\vec{b} = 3\hat{\imath} \hat{\jmath} 5\hat{k}$ .
- 9. Find the area of parallelogram whose diagonals are given by vectors:

(i) 
$$\vec{a} = 2\vec{i} + \vec{j} + \vec{k} \otimes \vec{b} = \vec{i} - \vec{k}$$

(ii) 
$$\vec{a} = \vec{i} + \vec{j} - 4\vec{k} \otimes \vec{b} = \vec{i} + 8\vec{j} + 2\vec{k}$$

10.Find the angle between the following vectors:

(i) 
$$-2i - 2j + 4k$$
 and  $-2i + 4j - 2k$ 

(ii) 
$$\bigwedge^{\wedge} \bigwedge^{\wedge} \bigwedge^{\wedge} \bigwedge^{\wedge} \bigwedge^{\wedge}$$
  
 $i + 2j + k \text{ and } 3i + 2j - 7k$ 

## 3/4 Marks Questions

- **1.** For any two vectors  $\vec{a}$  and  $\vec{b}$  prove that  $|\vec{a} \cdot \vec{b}| \le |\vec{a}||\vec{b}|$ . Also write the name of inequality.
- 2. For any two vectors  $\vec{a}$  and  $\vec{b}$  prove that  $|\vec{a} + \vec{b}| \le |\vec{a}| + |\vec{b}|$ . Also write the name of inequality.
- 3. Find the area of triangle whose vertices are :
  - (i) A(2,3,5), B(3,5,8), C(2,7,8)
  - (ii) A(1,2,4), B(3,1,-2), C(4,3,1)
  - (iii) P(1, 1, 1), Q(1, 2, 3), R(2, 3, 1)

4. Let  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  be three vectors such that  $|\vec{a}| = 3$ ,  $|\vec{b}| = 4$ ,  $|\vec{c}| = 5$  and each one of them is perpendicular to the sum of the other two, find  $|\vec{a} + \vec{b} + \vec{c}|$ .

- 5. If  $\vec{a} = 5\hat{\imath} + \hat{\jmath} 2\hat{k}$ ,  $\vec{b} = 7\hat{\imath} + 2\hat{\jmath} 3\hat{k}$ ,  $\vec{c} = 2\hat{\imath} 9\hat{\jmath} \hat{k}$  find a vector of magnitude 7 units parallel to the vector  $2\vec{a} \vec{b} + 3\vec{c}$ .
- 6. If  $\vec{a} = \hat{\imath} + 4\hat{\jmath} + 2\hat{k}$ ,  $\vec{b} = 3\hat{\imath} 2\hat{\jmath} + 7\hat{k}$ ,  $\vec{c} = 2\hat{\imath} \hat{\jmath} + 4\hat{k}$ , then find a vector  $\vec{d}$  which is perpendicular to both  $\vec{a}$  and  $\vec{b}$  and  $\vec{c} \cdot \vec{d} = 15$ .

## <u>UNIT – IV</u>

## **Three Dimensional Geometry**

# Multiple Choice Questions(1 Marks)

1	Direction ratios of straight line $\vec{r} = \hat{\iota} - 4\hat{j} + 5\hat{k} + s(2\hat{\iota} - 3\hat{j} + 2\hat{k})$ are	:
	(a) < 2,3,2 > (b) < 2, $-3, -2 >$ (c) < $-2, -3, 2 >$	( <b>d</b> )< 2,−3,2 >
2	Direction ratios of line given by $\frac{x-1}{3} = \frac{2y+6}{12} = \frac{1-z}{-7}$ are :	
	(a) $< 3,12,-7 >$ (b) $< 3,-6,7 >$ (c) $< 3,6,7 >$ (d) $< 3,6,-7 >$	>
3	Direction ratios of a line passing through the points $(-2, 1, 0)$ $\&$ $(3, 2, 1)$	are
	(a) $< 5,1,1 >$ (b) $< -5,1,-1 >$ (c) $< 5,-1,1 >$ (d) $< -$	5, -1, 1 >
4	Which of the following sets of points are collinear :	
	(a)(1,3,-4), (1,-2,7)&(3,8,-11) $(b)(2,3,-4), (2,-2,3)&(3,5,-1)$	-11)
	(c)(2,3,-4),(1,-2,3)&(3,8,-11)(d)(2,3,-4),(1,-2,3)&(2,8,11)	
5	Vector equation of the line $\frac{x+4}{5} = \frac{y-5}{3} = \frac{z-8}{-3}$ is	
	(a) $\vec{r} = 4\hat{\imath} - 5\hat{\jmath} - 8\hat{k} + \mu(5\hat{\imath} + 3\hat{\jmath} - 3\hat{k})$ (b) $\vec{r} = -4\hat{\imath} + 5\hat{\jmath} + 8\hat{k} + \mu(5\hat{\imath} + 3\hat{\jmath} - 3\hat{k})$	$5\hat{\imath}+3\hat{\jmath}-3\hat{k}$
	$(\mathbf{c})\vec{r} = 5\hat{\imath} + 3\hat{\jmath} - 3\hat{k} + \mu(4\hat{\imath} - 5\hat{\jmath} - 8\hat{k})(\mathbf{d})\vec{r} = 5\hat{\imath} + 3\hat{\jmath} - 3\hat{k} + \mu(-4\hat{\imath} - 4\hat{k})$	$+5\hat{j}-8\hat{k}$
6	Cartesian equation of the line $ec{r}=7m{\hat{\imath}}-5m{\hat{j}}+3m{\hat{k}}+\muig(9m{\hat{\imath}}-m{\hat{j}}+6m{\hat{k}}ig)$ is	
	$(a)\frac{x+9}{7} = \frac{y-1}{-5} = \frac{z+6}{3} \qquad (b)\frac{x-9}{7} = \frac{y+1}{-5} = \frac{z+6}{3}  (c)\frac{x+7}{9} = \frac{y-5}{-1} = \frac{z+3}{6}$	$(d)\frac{x-7}{9} = \frac{y+5}{-1} = \frac{z-3}{6}$
7	Angle between the lines $\frac{x+1}{2} = \frac{y-5}{-1} = \frac{z}{1}$ and $\frac{x}{2} = \frac{y+7}{5} = \frac{z-8}{-1}$ is	
	(a) $\pi/3$ (b) $\pi/2$ (c) $\pi/6$ (d)0	
8	Direction cosines of a line making equal angles with coordinate axes are	2
	(a) $< \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} >$ (b) $< \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >$ (c) $< 1, 1, 1 >$	(d)< 0,0,0 >
9	Direction ratios of a line making equal angles with coordinate axes are	
	(a) $< \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} >$ (b) $< \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}} >$ (c) $< 1, 1, 1 >$	(d)< 0,0,0 >
10	If direction ratios of a line are $< 9, -6, 2 >$ then its direction cosines are	•
	$(a) < \frac{9}{\sqrt{117}}, \frac{-6}{\sqrt{117}}, \frac{2}{\sqrt{117}} > \qquad (b) < \frac{9}{\sqrt{121}}, \frac{-6}{\sqrt{121}}, \frac{2}{\sqrt{121}} > (c) < \frac{9}{7}, \frac{-6}{7}, \frac{2}{7} > $	(d) $< \frac{9}{5}, \frac{-6}{5}, \frac{2}{5} >$

### 2/3 Marks Questions

- 1. Find the equation of a line which passes through the points (3, 6, -7) and (5, -1, 4).
- 2. Find the direction cosines of a line passing through the points (7, -1, 2) and (3, 4, -7).
- 3. Find the direction ratios and direction cosines of a line which makes equal angles with the coordinate axes.
- 4. Find the direction cosines of sides of a triangle whose vertices are (1, 2, -3), (9, -3, 7) and (5, 3, -2).
- 5. Find the angle between the lines :

(i) 
$$\vec{r} = 3\vec{i} + 8\vec{j} + 3\vec{k} + \mu\left(3\vec{i} - \vec{j} + \vec{k}\right) \otimes \vec{r} = -3\vec{i} - 7\vec{j} + 6\vec{k} + \lambda\left(-3\vec{i} + 2\vec{j} + 4\vec{k}\right)$$

(ii) 
$$\vec{r} = 2\vec{i} - \vec{j} - \vec{k} + \mu \left(3\vec{i} - 5\vec{j} + 2\vec{k}\right) \otimes \vec{r} = \vec{i} + 2\vec{j} + \vec{k} + \lambda \left(\vec{i} - \vec{j} + \vec{k}\right)$$

(iii)  $\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{1} \& \frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}$ 

(iv) 
$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} \& \frac{x-2}{3} = \frac{y-4}{5} = \frac{z-5}{5}$$

6. Find the value of *m* if the lines  $\frac{x+2}{3} = \frac{y-1}{2m} = \frac{z-2}{7}$  and  $\frac{x-3}{4} = \frac{y-2}{7} = \frac{z+5}{8m}$  are perpendicular to each other.

# 6/4 Marks Questions

1. Find the shortest distance between the following pairs of lines :

(i) 
$$\vec{r} = 3\vec{i} + 8\vec{j} + 3\vec{k} + \mu\left(3\vec{i} - \vec{j} + \vec{k}\right) \otimes \vec{r} = -3\vec{i} - 7\vec{j} + 6\vec{k} + \lambda\left(-3\vec{i} + 2\vec{j} + 4\vec{k}\right)$$

(ii) 
$$\vec{r} = 2 \vec{i} - \vec{j} - \vec{k} + \mu \left( 3 \vec{i} - 5 \vec{j} + 2 \vec{k} \right) \otimes \vec{r} = \vec{i} + 2 \vec{j} + \vec{k} + \lambda \left( \vec{i} - \vec{j} + \vec{k} \right)$$
  
(iii)  $\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{1} \otimes \frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}$ 

(iii) 
$$\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{1} \& \frac{x-2}{2} = \frac{y+1}{1} = \frac{z+1}{2}$$

(iv) 
$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} & \frac{x-2}{3} = \frac{y-4}{5} = \frac{z-5}{5}$$

(v) 
$$\frac{3-x}{2} = \frac{8-2y}{-10} = \frac{z-1}{1} & \frac{3x-6}{9} = \frac{5-y}{1} = \frac{4-2z}{8}$$

# <u>UNIT – V</u> <u>LINEAR PROGRAMMING</u> <u>Multiple Choice Questions(1 Mark)</u>

1	All points of feasible	region are :		
	(a)infeasible solution	s (b)feasible solutions	(c)optimal solutions	(d)none of these
2	Corner points of the	easible region are		
	(a)optimal solutions	(b)useless points	(c)infeasible solution	s (d)none of these
3	Common area for eac	h constraint is called :		
	(a)infeasible region	(b)feasible region	(c)useless area	(d)none of these
4	Maximum value of $Z$	= 4x + 3y subject to t	he constraints $x + y \leq 4$	$x, y \ge 0$ is
	(a)16	(b)12	(c)10	(d)20
5	Minimum value of Z	= 4x + 3y subject to tl	ne constraints $x + y \leq 4$ ,	$x, y \ge 0$ is
	(a)16	(b)12	(c)10	(d)20
6	Maximum value of $Z$	= 2x + 3y - 1 subject	to the constraints $x + y$	$\leq$ 5, $x, y \geq$ 0 is
	(a)14	(b)12	(c)10	(d)9
7	Minimum value of Z	= 5x + 3y + 2 subject	to the constraints $x + y$	$\leq$ 7, $x, y \geq$ 0 is
	(a)37	(b)35	(c)21	(d)23
8	Constraints of LPP are	2:		
	(a)Always quadratic		(b)/	Always linear
	(c)May be linear or q	uadratic depending on t	he problem (d)	May be cubic some times
9	Objective function of	LPP is		
	(a)Always quadratic		(b)/	Always linear
	(c)May be linear or q	uadratic depending on t	he problem (d)N	May be cubic some times
10	Minimum value of Z	= 5x + 3y + 2 subject	to the constraints $x + y$	$\leq$ 7, $x, y \geq$ 0 on the point
	(a)(7,0) (b)	(0,7)	(c)(3,4)	(d)(4,3)

## **4 Marks Questions**

Solve the following LPP graphically:

- 1. Maximize & Minimize :
  - (i) Z = 10x + 7y subject to the constraints  $3x + y \le 9$ ,  $3x + 2y \le 12$ ,  $x, y \ge 0$ .
  - (ii) Z = x + 2y subject to the constraints  $7x + 3y \le 21$ ,  $x + y \ge 3$ ,  $x y \le 0$ ,  $x, y \ge 0$ .
  - (iii) Z = 4x + 2y subject to the constraints  $8x + 9y \le 72$ ,  $4x + y \ge 8$ ,  $2x y \ge 0$ ,  $x, y \ge 0$ .
  - (iv) Z = 5x + 7y subject to the constraints  $x + y \ge 4$ ,  $x + 3y \le 12$ ,  $x 2y \ge 0$ ,  $x, y \ge 0$ .
  - (v) Z = 3x + 6y subject to the constraints  $x + y \le 6$ ,  $2x + y \ge 6$ ,  $2x y \le 0$ ,  $x, y \ge 0$ .
  - (vi) Z = 4x + 5y subject to the constraints  $x + y \le 6$ ,  $2x + y \ge 6$ ,  $x y \ge 0$ ,  $x, y \ge 0$ .
  - (vii) Z = 8x + y subject to the constraints  $x + y \le 8$ ,  $2x + y \ge 8$ ,  $x 2y \le 0$ ,  $x, y \ge 0$ .
  - (viii) Z = 3x + 7y subject to the constraints  $x + y \le 10$ ,  $x + 2y \ge 6$ ,  $3x y \le 9$ ,  $x, y \ge 0$ .
  - (ix) Z = 8x + 5y 2 subject to the constraints  $x + y \le 10$ ,  $x + 2y \ge 6$ ,  $3x y \ge 9$ ,  $x, y \ge 0$
  - (x) Z = 7x + 5y 1 subject to the constraints  $x + y \le 10, x + y \ge 5, x y \le 0, x, y \ge 0$

# <u>UNIT – VI</u>

# PROBABILITY Multiple Choice Questions(1 Mark)

1	If $P(A) = \frac{1}{2}$ , $P(A) = \frac{1}{2}$	$(B) = \frac{3}{8}$ and $P(A \cap B) =$	$=\frac{1}{5}$ then $P(A B)$ is equ	al to :	
	(a) <sup>2</sup> 5	(b) $\frac{8}{15}$	(c) $\frac{2}{3}$		(d) $\frac{5}{8}$
2	If A and B are in	dependent events and I	$P(A) = \frac{1}{2}$ , $P(B) = \frac{3}{8}$	then $P(A \cap$	B)is equal to :
	(a) <sup><u>3</u></sup>	(b) $\frac{3}{8}$		-	(d) $\frac{1}{16}$
3	$If P(A) = \frac{1}{2} , P(A)$	$(B) = \frac{3}{8}$ and $P(A \cap B) =$	10	al to :	10
	(a) <sup>2</sup>	8 (b) <u>8</u>	(c) $\frac{2}{2}$		(d) $\frac{5}{2}$
4	5	tting even prime numbe	3	hrow of a pai	δ
	(a)1/6	(b)2/35	(c)	1/36	(d)5/36
5	$If P(A) = \frac{1}{2} , P(A) = \frac{1}{2} $	$(B) = \frac{3}{8}$ and $P(A \cup B) =$	$=rac{4}{5}$ then $P(A B)$ is equ	al to :	
	(a) <sup>1</sup> / <sub>5</sub>	(b) $\frac{8}{15}$	(c) $\frac{2}{3}$		(d)
6	If E is any event	then P(E) belongs to the	e interval :		
	(a)(1,10)	(b) $(0, 1)$	(c) [0, 1]		(d) [10, 20]
7	If $P(E) = \frac{5}{7}$ then	P(not E) is			
	(a) <sup>5</sup> 7	(b) <sup>7</sup> 5	(c)	$\frac{7}{2}$	(d) $\frac{2}{7}$
8	1	with head on both side	s then on tossing the	coin probabi	ity of getting head is :
	(a) <sup><u>1</u></sup>	(b)0	(c)1		(d)2
9		tting an ace card on dra		well shuffled	
	(a)1/13	(b)1/4	(c)1/52		(d)none of these
10	<b>n</b>	Mondays in a leap year $u^2$	1	<i>.</i> 1	
	$(a)\frac{2}{53}$	(b) <sup>2</sup> /7	$(c)\frac{1}{53}$	(d) <sup>1</sup> 7	
11	•	Mondays in a non-leap	1	<i>i</i> 1	
	(a) <sup>2</sup> / <sub>53</sub>	(b) <sup>2</sup> /7	(c) $\frac{1}{53}$	$(d)\frac{1}{7}$	
12	-	then $P(not E)$ belongs			
40	(a)(1,10)	(b) (0, 1)	(c) [0, 1]	(d) [10, 2	0]
13	•	e tossed once, then gett	-		
	(a) <sup>3</sup> / <sub>8</sub>	(b) <sup>7</sup> /8	$(c)\frac{5}{8}$	$(d)\frac{1}{2}$	
14		calls, 4 white balls and 7 awing a white ball is	blue balls in a bag. O	one ball is dra	wn at random from the bag.
	(a) $\frac{2}{7}$	(b) $\frac{3}{14}$	(c) $\frac{7}{14}$	(d)0	
15	/	14	11		wn at random from the bag.
15		awing a green ball is	blue balls in a bag. O		wil at landom nom the bag.
	(a) <sup>2</sup> / <sub>7</sub>	(b) $\frac{3}{14}$	$(c)\frac{7}{14}$	(d)0	
16	/	dependent events , ther	17		
	$(a)P(E\cup F)=P$	-	$(c)P(E \cap F) = F$	P(E) + P(F)	
	(c) $P(E \cap F) = I$	P(E). P(F)	(d) $P(E \cap F) =$	0	
			- ill in the Blanks(	1 Mark)	
		<u>י</u>		<u> 1 IVIAI NJ</u>	

29) If 
$$P(A) = \frac{1}{5}$$
 then  $P(not A) =$ \_\_\_\_\_

30) In a throw of a pair of dice probability of getting a doublet is \_\_\_\_\_

- 31) Probability of occurrence of sure event = \_\_\_\_\_
- 32) Probability of occurrence of impossible event = \_\_\_\_\_

**33)** 
$$P(A \cup B) = P(A) + P(B) -$$
\_\_\_\_\_

- 34)  $P(A) + \_\_\_ = 1$
- 35) If *A* and *B* are independent events then  $P(A \cap B) =$ \_\_\_\_\_
- 36) If  $P(A) = \frac{1}{2}$  and P(B) = 0 then P(A|B) is \_\_\_\_\_
- 37) If a dice is tossed once then probability of getting an odd prime number is \_\_\_\_\_
- 38) Probability of any event is (numerically) always less than or equal to \_\_\_\_\_\_

## **4 Marks Questions**

- **1.** If  $P(A) = \frac{6}{11}$ ,  $P(B) = \frac{5}{11}$  and  $P(A \cup B) = \frac{7}{11}$  then find :  $P(A \cap B)$ , P(A/B) & P(B/A)
- 2. If P(E) = 0.45, P(F) = 0.55 &  $P(E \cup F) = 0.75$  then find  $P(E \cap F)$  & P(E/F).
- 3. If *A* & *B* are independent events and :
  - (i) If P(A) = 0.4,  $P(A \cup B) = 0.7$  then find P(B).
  - (ii) if P(A) = 0.5,  $P(A \cup B) = 0.7$  then find P(B).
- 4. An urn contains 7 red and 4 blue balls. Two balls are drawn at random with replacement. Find the probability of getting : (a) 2 red balls, (b) 2 blue balls.
- 5. A bag contains 3 white and 5 black balls. Two balls are drawn at random without replacement. Determine the probability of getting the black balls.
- 6. A husband and wife appear in an interview for two vacancies in the same post. The probability of husband's selection is 1/7 and that of wife's is 1/5. Find the probability that (a) both get selected (b) only one of them get selected.
- 7. The probability of A hitting a target is 4/5 and that of B is 2/3. They both fire at the target. Find the probability that : (a) at least one of them will hit the target, (b) only one of them will hit the target.
- 8. A problem is given to 3 students whose chances of solving it are 1/3, 1/5 and 1/6. What is the probability that (i) exactly one of them may solve it, (ii) the problem will be solved.
- 9. A problem is given to 3 students whose chances of solving it are 1/3, 1/5 and 1/6. What is the probability that (i) exactly two of them may solve it, (ii) at least two of them will solve it, (iii) problem will be solved.
- 10. Two bags contain 6 red and 4 black balls, 3 red and 3 black balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from first bag.
- 11. Two bags contain 7 red and 2 black balls, 3 red and 6 black balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from first bag.
- 12. In a factory which manufactures bolts, machine A, B and C manufacture respectively 25%, 35% and 40% of the bolts. Of their outputs 5%, 4% and 2% are respectively defective bolts. A bolt is drawn at random from the product and is found to be defective. What is the probability that it is manufactured by the machine B.

Prepared By :Vaibhav , Lecturer(Maths), Govt. Multipurpose Sen. Sec. School, Patiala

### CLASS-XII(2024-25)

### MATHEMATICS

## Time: 3 Hrs

### Theory: 80 Marks INA: 20 Marks Total: 100 Marks

- 1. All the questions are compulsory.
- 2. The question paper consists of 19 questions divided into 4 sections A, B, C and D.
- 3. Section A comprises of 2 questions.
  - i. Q.No.1 consists of 15 Multiple Choice Questions carrying 1 mark each.
  - ii. Q.No.2 consists of 5 Fill in the blank type questions carrying 1 mark each.
- 4. Section B comprises of 7 questions of 2 marks each.
- 5. Section C comprises of 7 questions of 4 marks each.
- 6. Section D comprises of 3 questions of 6 marks each.
- 7. An internal choice has been provided in three questions of 2 marks, three questions of 4 marks and three questions of 6 marks each. You have to attempt only one of the alternatives in all such questions.
- 8. Use of calculators is not permitted.

Sr. No.	UNIT	CHAPTERS	Q. Carrying 1-Mark	Q. Carrying 2-Marks	Q. Carrying 4-Marks	Q. Carrying 6-Marks	Total Marks
		Relations &					
1	Relations &	Functions					_
	Functions	Inverse	3	-	1	-	7
		Trigonometric					
		Functions					
2	Algebra	Matrices	- 3	1	1	1	15
		Determinants	_				_
	Calculus	Continuity and					35
		Differentiability	_				
		Applications of					
3		Derivatives					
3		Integrals	7	5	3	1	
		Applications of					
		the Integrals					
		Differential					
		Equations					
	Vectors and	Vectors					
4	Three	Three	4	1	_	1	12
	Dimensional	Dimensional		1	_	1	14
	Geometry	Geometry					
5	Linear	Linear	1	_	1	_	5
	Programming	Programming		_		_	
6	Probability	Probability	2	-	1	-	6
	TOTAL		2(20)	7	7	3	19
		QUESTIONS	2(20)			5	19
		TOTAL MARKS	20	14	28	18	80

MODEL TEST PAPER 2024-25 MATHEMATICS(10+2)

**TIME ALLOWED: 3 hours** 

MAX. MARKS:80

### Instructions:

- 1. All the questions are compulsory.
- 2. The question paper consists of 19 questions divided into 4 sections A,B,C and D.
- 3. Section A comprises of 2 questions:
  - (i) Q.No.1 consists of 15 Multiple Choice Questions carrying 1 mark each.
  - (ii) Q.No.2 consists of 5 Fill in the Blank type questions carrying 1 mark each.
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- 5. Section C comprises of 7 questions of 4 marks each.
- 6. Section D comprises of 3 questions of 6 marks each.
- 7. Internal choice has been provided in three questions of 2 marks, three questions of 4 marks and three questions of 6 marks each. You have to attempt only one of the alternatives in all such questions.
- 8. Use of calculator is not permitted.

#### SECTION – A

### Q1 Choose the correct options in the following questions:

(i)	Function $f: N \rightarrow N$ , $f(x)$ (A)one-one only	$x) = x^2 + 1 \text{ is :}$ (B)onto only (C)	one-one and onto	(D)neither one-one nor onto	1
(ii)	Relation given by $R = \{$ (A)reflexive only	(b, b), (g, g), (g, s), (s, g (B)symmetric only	(C) $\{b, g\}$ in the set $A = \{b, g\}$	g, s} is : (D) equivalence relation	1
(iii)	If $\begin{vmatrix} 1 & -x \\ 4 & -4 \end{vmatrix} = \begin{vmatrix} x & 8 \\ 4 & -3 \end{vmatrix}$ (A)8	, then value of x is: (B)-4	(C)3	(D)-8	1
(iv)	If order of matrix A' is $2 \times 3$ and order of matrix B is $3 \times 5$ then order of matrix B'A is:				
( )	$(A)5 \times 2$	(B) 2 × 5	(C) 5 × 3	(D) 3 × 2	
(v)	If $y = log x$ , then $y''$ is (A)1		(C) $\frac{1}{x^2}$	(D) $-\frac{1}{x^2}$	1
(vi)	Critical point of the function $(A)x = 4$	nction $f(x) = x^2 - 10$ (B) $x = 6$	x + 2 is: (C) $x = 5$	(D) $x = 2$	1
(vii)	$\int e^{2\log x} dx$ is equal to: (A) $x + c$	$(B)\frac{x^2}{2} + c$	$(C)\frac{x^3}{3} + c$	$(D)\frac{x^4}{4} + c$	1
(viii)	$\int_{-1}^{1} x^{2024} dx$ is equal to:	(B) $\frac{1}{2024}$	(C) $\frac{2}{2025}$	(D) $\frac{1}{2025}$	1
	(A)0		2025	\$ 2025	
(ix)	Degree of differential e (A)3	(B) 2	(C)	(D) not defined	1
(x)	$y = e^{2x}$ is solution of d (A) $y'' - y' = 0$	ifferential equation $g$ (B) $y'' - 4y' = 0$	given by: (C) $y'' + y' = 0$	(D) $y'' - 2y' = 0$	1
(xi)	If $\vec{a} \cdot \vec{b} = -\frac{1}{c}  \vec{a} \times \vec{b} $ then angle between vector $\vec{a}$ and vector $\vec{b}$ is :				
	(A) $\frac{\pi}{2}$	(B) $\frac{\pi}{6}$	(C) $\frac{\pi}{4}$	(D) $\frac{2\pi}{3}$	1
(xii)	If $\vec{a}.\vec{b} = 0$ then angle (A) $\frac{\pi}{2}$	(B) $\frac{2}{6}$	$(C) - \frac{1}{4}$	(D) $\frac{\pi}{3}$	1
(xiii)	Direction ratios of line	e given by $\frac{x-1}{3} = \frac{2y+6}{12}$	$=\frac{1-z}{-7}$ are :		1
	(A) < 3.12, -7 >	(B) < 3, −6,7 >	(C) < 3,6,7 >	(D)< 3,6, -7 >	1
(xiv)	Common area for each	Inteasible region	10/40010000	on (D)main region	1
$(\mathbf{x}\mathbf{v})$	(A) inteasible region If $P(A) = \frac{1}{2}$ , $P(B) = \frac{3}{8}$	and $P(A \cap B) = \frac{1}{5}$ the	en P(A/B) is equal to	(D) <sup>5</sup> / <sub>8</sub>	1
	$(A)^{\frac{2}{5}}$	(B) $\frac{8}{15}$	(C) $\frac{2}{3}$		

Q2 Fill in the blanks:						
(i) $\cos^{-1}\left(\cos\frac{5\pi}{3}\right) =$						
(ii) If $A = [a_{ij}]_{2\times 3}$ such that $a_{ij} = - i-j $ then $a_{12} = -\frac{\pi}{3}$						
(11) $\int_{\pi/4} \cot x  dx =$						
(iv) If a line makes angles $135^{\circ}$ , $90^{\circ}$ , $45^{\circ}$ with x,y,z axes respectively, then its direction cosines	1					
(v) If A and B are independent events such that $P(B) = 0.3$ , $P(A \cap B) = 0.12$ , then $P(A) =$						
SECTION – B						
Q3 If the area of triangle is 3 square units with vertices(2,0), (0,0) and (1,k), then find k. Q4 If $y = sin^{-1} \left( cos \frac{x}{2} \right)$ , then find $\frac{dy}{dx}$	2					
Q5 Find the interval in which function $f(x) = x^2 + 4x + 7$ is decreasing.	2 2					
An edge of a variable cube is increasing at the rate of 4 cm/s. How fast is the volume of th cube increasing when the edge is 20cm long? Q6 Evaluate $\int_{\pi/6}^{\pi/3} \frac{dx}{1+\sqrt{\tan x}}$ .	2					
OR	2					
Evaluate $\int \frac{1}{\sqrt{16-9x^2}} dx$	2					
Q7 Find the general solution of the differential equation $\frac{dy}{dx} = (4 + y^2)(1 + 3x^2)$	2					
Q8 Using integration find the area bounded by the parabola $y^2 = 8x$ straight lines $x = 2, x = 5$ is the first quadrant.	in					
Q9 Find the value of $\lambda$ if the vectors $\vec{a} = 2\hat{i} - \hat{j} - \lambda \hat{k}$ and $\vec{b} = 5\hat{i} - \hat{j} + 2\hat{k}$ are perpendicular to each	2 h					
other. OR	2					
Find the angle between the lines : $\frac{x-2}{1} = \frac{y-3}{2} = \frac{z-7}{-5}$ and $\frac{x+5}{3} = \frac{y-2}{2} = \frac{z-6}{4}$	2					
SECTION – C						
Q10 Prove that $\cos^{-1}\frac{12}{13} + \sin^{-1}\frac{3}{5} = \sin^{-1}\frac{56}{65}$	4					
Q11 If $2X + 3Y = \begin{bmatrix} 5 & -6 \\ 0 & 4 \end{bmatrix}$ and $3X + 2Y = \begin{bmatrix} 3 & -3 \\ 7 & 1 \end{bmatrix}$ , then find X and Y	4					
Q12 Differentiate $x^{\log x} + (\log x)^x$ w.r.t. x	4					
OR						
If $x = 3\left(\cos\theta + \log\tan\frac{\theta}{2}\right)$ , $y = 5\sin\theta$ , then find $\frac{dy}{dx}$	4					
Q13 Evaluate $\int_{0}^{4} ( x-2 + x ) dx$	4					
Evaluate $\int \left[\log(\log x) + \frac{1}{(\log x)^2}\right] dx$	4					
Q14 Find the particular solution of the differential equation $\frac{dy}{dx} + 2y \tan x = \sin x$ ; $y = 0$ when $x = \frac{\pi}{3}$	4					
Q15 Solve the following linear programming problem graphically: Maximize and minimize $Z = 4x + 3y$ subject to the constraints						
$x + y \le 10$ , $5x + 2y \ge 10$ , $3y \ge x$ , $x \ge 0$ , $y \ge 0$	4					

Probability of solving a specific problem independently by A and B are 1/3 and 1/2 respectively. If both try to solve the problem independently, find the probability that: (i)the problem is solved (ii)exactly one of them solves the problem

#### OR

An insurance company insures 2000 scooter drivers, 4000 car drivers and 6000 truck drivers. The probability of accidents is 0.01, 0.03 and 0.15 respectively. One of the insured persons meets with an accident. What is the probability that he is a truck driver ?

#### **SECTION – D**

Q17(a) Express the matrix 
$$A = \begin{bmatrix} 2 & -3 & 5 \\ 8 & -7 & 9 \\ -6 & 5 & -4 \end{bmatrix}$$
 as a sum of a symmetric matrix and a skew-4

symmetric matrix.

(b) If 
$$A = \begin{bmatrix} 3 & -2 \\ 4 & -2 \end{bmatrix}$$
 then find k so that  $A^2 + 2I = kA$   
OR

Solve the following system of linear equations by matrix method: 3x - 7y - 2z = 29, 2x + 5y - 3z = -39, 4x + 2z - 2y = 30

Q18 Find the height of the cone of greatest volume that can be inscribed in a sphere of radius 30 cm.

Solve  $\int \frac{x^2}{x^4+1} dx$ 

Q19(a) Find the projection of the vector \$\vec{a} = 3\hlow{i} - 2\hlow{j} + 7\hlow{k}\$ on the vector \$\vec{b} = 6\hlow{i} + \hlow{j} - 2\hlow{k}\$
 (b) Find any diagonal of the parallelogram whose adjacent sides are given by the vectors \$\vec{a} = 5\hlow{i} + 2\hlow{j} + \hlow{k}\$ and \$\vec{b} = \hlow{i} + 9\hlow{j} + 2\hlow{k}\$. Also find the area of the parallelogram. OR

Find the shortest distance between the lines

$$\frac{x-1}{-1} = y + 2 = \frac{3-z}{2}$$
 and  $x - 1 = \frac{y+1}{2} = \frac{z+1}{-2}$ 

Q16

4

4

2

6

6

6

2

4

6